

# Numbers

## Prime Factors, Highest Common Factors, and Lowest Common Multiples - Memo

1. Find all the prime factors of the following numbers using the ladder method:

a) 
$$\begin{array}{c|c} 179 & 179 \\ \hline 1 & \end{array}$$

b) 
$$\begin{array}{c|c} 276 & 2 \\ \hline 138 & 2 \\ 69 & 3 \\ \hline 23 & 23 \\ 1 & \end{array}$$

c) 
$$\begin{array}{c|c} 186 & 2 \\ \hline 93 & 3 \\ 31 & 31 \\ \hline 1 & \end{array}$$

d) 
$$\begin{array}{c|c} 147 & 3 \\ \hline 49 & 7 \\ 7 & 7 \\ \hline 1 & \end{array}$$

e) 
$$\begin{array}{c|c} 81 & 3 \\ \hline 27 & 3 \\ 9 & 3 \\ 3 & 3 \\ \hline 1 & \end{array}$$

f) 
$$\begin{array}{c|c} 171 & 3 \\ \hline 57 & 3 \\ 19 & 19 \\ \hline 1 & \end{array}$$

g) 
$$\begin{array}{c|c} 64 & 2 \\ \hline 32 & 2 \\ 16 & 2 \\ 8 & 2 \\ 4 & 2 \\ \hline 2 & 2 \\ 1 & \end{array}$$

h) 
$$\begin{array}{c|c} 102 & 2 \\ \hline 51 & 3 \\ 17 & 17 \\ \hline 1 & \end{array}$$

i) 
$$\begin{array}{c|c} 22 & 2 \\ \hline 11 & 11 \\ 1 & \end{array}$$

j) 
$$\begin{array}{c|c} 214 & 2 \\ \hline 107 & 107 \\ 1 & \end{array}$$

k) 
$$\begin{array}{c|c} 264 & 2 \\ \hline 132 & 2 \\ 66 & 2 \\ 33 & 3 \\ 11 & 11 \\ 1 & \end{array}$$

l) 
$$\begin{array}{c|c} 159 & 3 \\ \hline 53 & 53 \\ 1 & \end{array}$$
  
m) 
$$\begin{array}{c|c} 185 & 5 \\ \hline 37 & 37 \\ 1 & \end{array}$$

n) 
$$\begin{array}{c|c} 153 & 3 \\ \hline 51 & 3 \\ 17 & 17 \\ 1 & \end{array}$$

o) 
$$\begin{array}{c|c} 162 & 2 \\ \hline 81 & 3 \\ 27 & 3 \\ 9 & 3 \\ 3 & 3 \\ 1 & \end{array}$$

p) 
$$\begin{array}{c|c} 256 & 2 \\ \hline 128 & 2 \\ 64 & 2 \\ 32 & 2 \\ 16 & 2 \\ 8 & 2 \\ 4 & 2 \\ 2 & 2 \\ 1 & \end{array}$$

q) 
$$\begin{array}{c|c} 268 & 2 \\ \hline 134 & 2 \\ 67 & 67 \\ 1 & \end{array}$$
  
r) 
$$\begin{array}{c|c} 127 & 127 \\ \hline 1 & \end{array}$$

s)	161	7
	23	23
	1	

t)	300	2
	150	2
	75	5
	15	5
	3	3
	1	

2. Find all the prime factors of the following numbers using the tree/branch method:

a) 291

```

  291
  /   \
  3   97
  
```

b) 60

```

  60
  /   \
  5   12
      /   \
      2   6
          / \
          2   3
  
```

c) 90

```

  90
  /   \
  3   30
      / \
      3   10
          / \
          5   2
  
```

d) 174

```

  174
  /   \
  2   87
      / \
      3   29
  
```

e) 81

```

  81
  / \
  3   27
      / \
      3   9
          / \
          3   3
  
```

f) 97

```

  97
  / \
  1   97
  
```

g) 200

```

  200
  /   \
  2   100
      /   \
      2   50
          /   \
          2   25
              / \
              5   5
  
```

h) 16

```

  16
  /   \
  2   8
      /   \
      2   4
          / \
          2   2
  
```

i) 
$$\begin{array}{ccc} 185 & & \\ \swarrow 5 & \searrow 37 & \\ & & \end{array}$$

j) 
$$\begin{array}{cccccc} 275 & & & & & \\ \swarrow 5 & \searrow 5 & \swarrow 5 & \searrow 11 & & \\ & & & & & \end{array}$$

k) 
$$\begin{array}{ccccc} 88 & & & & \\ \swarrow 11 & \searrow 8 & & & \\ \swarrow 2 & \searrow 4 & & & \\ \swarrow 2 & \searrow 2 & & & \\ & & & & \end{array}$$

l) 
$$\begin{array}{ccc} 143 & & \\ \swarrow 11 & \searrow 13 & \\ & & \end{array}$$

m) 
$$\begin{array}{cc} 95 & \\ \swarrow 5 & \searrow 19 & \\ & & \end{array}$$

n) 
$$\begin{array}{ccc} 63 & & \\ \swarrow 3 & \searrow 21 & \\ \swarrow 3 & \searrow 7 & \\ & & \end{array}$$

o) 
$$\begin{array}{ccccc} 36 & & & & \\ \swarrow 2 & \searrow 18 & & & \\ \swarrow 2 & \searrow 9 & & & \\ \swarrow 3 & \searrow 3 & & & \\ & & & & \end{array}$$

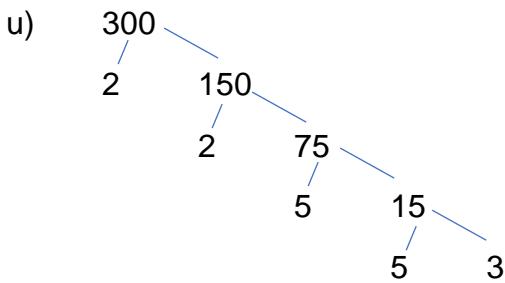
p) 
$$\begin{array}{ccccc} 264 & & & & \\ \swarrow 2 & \searrow 132 & & & \\ \swarrow 2 & \searrow 66 & & & \\ \swarrow 2 & \searrow 33 & & & \\ \swarrow 3 & \searrow 11 & & & \\ & & & & \end{array}$$

q) 
$$\begin{array}{ccc} 246 & & \\ \swarrow 2 & \searrow 123 & \\ \swarrow 3 & \searrow 41 & \\ & & \end{array}$$

r) 
$$\begin{array}{ccc} 70 & & \\ \swarrow 2 & \searrow 35 & \\ \swarrow 5 & \searrow 7 & \\ & & \end{array}$$

s) 
$$\begin{array}{ccccc} 228 & & & & \\ \swarrow 2 & \searrow 114 & & & \\ \swarrow 2 & \searrow 57 & & & \\ \swarrow 3 & \searrow 19 & & & \\ & & & & \end{array}$$

t) 
$$\begin{array}{ccccc} 180 & & & & \\ \swarrow 2 & \searrow 90 & & & \\ \swarrow 2 & \searrow 45 & & & \\ \swarrow 5 & \searrow 9 & & & \\ \swarrow 3 & \searrow 3 & & & \\ & & & & \end{array}$$



3. Find the highest common factor (or greatest common divisor) for each of the pairs of numbers.

a) 171 and 152

$$171 = 3 \times 3 \times 19$$

$$152 = 2 \times 2 \times 2 \times 19$$

$$\mathbf{HCF = 19}$$

b) 23 and 42

$$23 = 23 \times 1$$

$$42 = 2 \times 3 \times 7$$

$$\mathbf{HCF = 1}$$

c) 105 and 77

$$105 = 3 \times 5 \times 7$$

$$77 = 7 \times 11$$

$$\mathbf{HCF = 7}$$

d) 221 and 247

$$221 = 13 \times 17$$

$$247 = 13 \times 19$$

$$\mathbf{HCF = 13}$$

e) 96 and 224

$$96 = 2 \times 2 \times 2 \times 2 \times 2 \times 3$$

$$224 = 2 \times 2 \times 2 \times 2 \times 2 \times 7$$

$$\mathbf{HCF = 2 \times 2 \times 2 \times 2 \times 2 = 32}$$

f) 114 and 285

$$114 = 2 \times 3 \times 19$$

$$285 = 3 \times 5 \times 19$$

$$\mathbf{HCF = 3 \times 19 = 57}$$

g) 44 and 121

$$44 = 2 \times 2 \times 11$$

$$121 = 11 \times 11$$

$$\mathbf{HCF = 11}$$

h) 278 and 780

$$278 = 2 \times 139$$

$$780 = 2 \times 2 \times 3 \times 5 \times 13$$

$$\mathbf{HCF = 2}$$

i) 110 and 88

$$110 = 2 \times 5 \times 11$$

$$88 = 2 \times 2 \times 2 \times 11$$

$$\mathbf{HCF = 2 \times 11 = 22}$$

j) 216 and 36

$$216 = 2 \times 2 \times 2 \times 3 \times 3 \times 3$$

$$36 = 2 \times 2 \times 3 \times 3$$

$$\mathbf{HCF = 2 \times 2 \times 3 \times 3 = 36}$$

k) 75 and 90

$$75 = 3 \times 5 \times 5$$

$$90 = 2 \times 3 \times 3 \times 5$$

$$\mathbf{HCF = 3 \times 5 = 15}$$

l) 65 and 104

$$65 = 5 \times 13$$

$$104 = 2 \times 2 \times 2 \times 13$$

$$\mathbf{HCF = 13}$$

m) 252 and 210

$$252 = 2 \times 2 \times 3 \times 3 \times 7$$

$$210 = 2 \times 3 \times 5 \times 7$$

$$\mathbf{HCF = 2 \times 3 \times 7 = 42}$$

n) 175 and 200

$$175 = 5 \times 5 \times 7$$

$$200 = 2 \times 2 \times 2 \times 5 \times 5$$

$$\mathbf{HCF = 5 \times 5 = 25}$$

o) 172 and 258

$$172 = 2 \times 2 \times 43$$

$$258 = 2 \times 3 \times 43$$

$$\mathbf{HCF = 2 \times 43 = 86}$$

4. Find the highest common factor (or greatest common divisor) for each of these sets of numbers

a) 217, 147 and 126

$$217 = 7 \times 31$$

$$147 = 3 \times 7 \times 7$$

$$126 = 2 \times 3 \times 3 \times 7$$

$$\mathbf{HCF = 7}$$

b) 195, 390 and 520

$$195 = 3 \times 5 \times 13$$

$$390 = 2 \times 3 \times 5 \times 13$$

$$520 = 2 \times 2 \times 2 \times 5 \times 13$$

$$\mathbf{HCF = 5 \times 13 = 65}$$

c) 50, 36 and 100

$$50 = 2 \times 5 \times 5$$

$$36 = 2 \times 2 \times 3 \times 3$$

d) 22, 33 and 88

$$22 = 2 \times 11$$

$$33 = 3 \times 11$$

$$100 = 2 \times 2 \times 5 \times 5$$

$$\mathbf{HCF = 2}$$

$$88 = 2 \times 2 \times 2 \times 11$$

$$\mathbf{HCF = 11}$$

e) 16, 24 and 48

$$16 = 2 \times 2 \times 2 \times 2$$

$$24 = 2 \times 2 \times 2 \times 3$$

$$48 = 2 \times 2 \times 2 \times 2 \times 3$$

$$\mathbf{HCF = 2 \times 2 \times 2 = 8}$$

f) 91, 343 and 210

$$91 = 7 \times 13$$

$$343 = 7 \times 7 \times 7$$

$$210 = 2 \times 3 \times 5 \times 7$$

$$\mathbf{HCF = 7}$$

g) 228, 285 and 399

$$228 = 2 \times 2 \times 3 \times 19$$

$$285 = 3 \times 5 \times 19$$

$$399 = 3 \times 7 \times 19$$

$$\mathbf{HCF = 3 \times 19 = 57}$$

h) 60, 144 and 336

$$60 = 2 \times 2 \times 3 \times 5$$

$$144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3$$

$$336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7$$

$$\mathbf{HCF = 2 \times 2 \times 3 = 12}$$

i) 255, 102 and 306

$$255 = 3 \times 5 \times 17$$

$$102 = 2 \times 3 \times 17$$

$$306 = 2 \times 3 \times 3 \times 17$$

$$\mathbf{HCF = 3 \times 17 = 51}$$

j) 290, 580 and 145

$$290 = 2 \times 5 \times 29$$

$$580 = 2 \times 2 \times 5 \times 29$$

$$145 = 5 \times 29$$

$$\mathbf{HCF = 5 \times 29 = 145}$$

5. Find the lowest common multiple for each of these pairs of numbers

a) 171 and 152

$$171 = 3 \times 3 \times 19$$

$$152 = 2 \times 2 \times 2 \times 19$$

$$\mathbf{LCM = 2 \times 2 \times 2 \times 3 \times 3 \times 19}$$

$$\mathbf{LCM = 1 368}$$

b) 23 and 42

$$23 = 23 \times 1$$

$$42 = 2 \times 3 \times 7$$

$$\mathbf{LCM = 2 \times 3 \times 7 \times 23}$$

$$\mathbf{LCM = 966}$$

c) 105 and 77

$$105 = 3 \times 5 \times 7$$

$$77 = 7 \times 11$$

$$\text{LCM} = 3 \times 5 \times 7 \times 11$$

$$\text{LCM} = 1\,155$$

d) 221 and 247

$$221 = 13 \times 17$$

$$247 = 13 \times 19$$

$$\text{LCM} = 13 \times 17 \times 19$$

$$\text{LCM} = 4\,199$$

e) 96 and 224

$$96 = 2 \times 2 \times 2 \times 2 \times 2 \times 3$$

$$224 = 2 \times 2 \times 2 \times 2 \times 2 \times 7$$

$$\text{LCM} = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 7$$

$$\text{LCM} = 672$$

f) 114 and 285

$$114 = 2 \times 3 \times 19$$

$$285 = 3 \times 5 \times 19$$

$$\text{LCM} = 2 \times 3 \times 5 \times 19$$

$$\text{LCM} = 570$$

g) 44 and 121

$$44 = 2 \times 2 \times 11$$

$$121 = 11 \times 11$$

$$\text{LCM} = 2 \times 2 \times 11 \times 11$$

$$\text{LCM} = 484$$

h) 278 and 780

$$278 = 2 \times 139$$

$$780 = 2 \times 2 \times 3 \times 5 \times 13$$

$$\text{LCM} = 2 \times 2 \times 3 \times 5 \times 13 \times 139$$

$$\text{LCM} = 108\,420$$

i) 110 and 88

$$110 = 2 \times 5 \times 11$$

$$88 = 2 \times 2 \times 2 \times 11$$

$$\text{LCM} = 2 \times 2 \times 2 \times 5 \times 11$$

$$\text{LCM} = 440$$

j) 216 and 36

$$216 = 2 \times 2 \times 2 \times 3 \times 3 \times 3$$

$$36 = 2 \times 2 \times 3 \times 3$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 \times 3 \times 3$$

$$\text{LCM} = 216$$

k) 75 and 90

$$75 = 3 \times 5 \times 5$$

$$90 = 2 \times 3 \times 3 \times 5$$

$$\text{LCM} = 2 \times 3 \times 3 \times 5 \times 5$$

$$\text{LCM} = 450$$

l) 65 and 104

$$65 = 5 \times 13$$

$$104 = 2 \times 2 \times 2 \times 13$$

$$\text{LCM} = 2 \times 2 \times 2 \times 5 \times 13$$

$$\text{LCM} = 520$$

m) 252 and 210

$$252 = 2 \times 2 \times 3 \times 3 \times 7$$

$$210 = 2 \times 3 \times 5 \times 7$$

$$\text{LCM} = 2 \times 2 \times 3 \times 3 \times 5 \times 7$$

$$\text{LCM} = 1\,260$$

n) 175 and 200

$$175 = 5 \times 5 \times 7$$

$$200 = 2 \times 2 \times 2 \times 5 \times 5$$

$$\text{LCM} = 2 \times 2 \times 2 \times 5 \times 5 \times 7$$

$$\text{LCM} = 1\,400$$

o) 172 and 258

$$172 = 2 \times 2 \times 43$$

$$258 = 2 \times 3 \times 43$$

$$\text{LCM} = 2 \times 2 \times 3 \times 43$$

$$\text{LCM} = 516$$

6. Find the lowest common multiple for each of these sets of numbers

a) 217, 147 and 126

$$217 = 7 \times 31$$

$$147 = 3 \times 7 \times 7$$

$$126 = 2 \times 3 \times 3 \times 7$$

b) 195, 390 and 520

$$195 = 3 \times 5 \times 13$$

$$390 = 2 \times 3 \times 5 \times 13$$

$$520 = 2 \times 2 \times 2 \times 5 \times 13$$

$$\text{LCM} = 2 \times 3 \times 3 \times 7 \times 7 \times 31$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 \times 5 \times 13$$

$$\text{LCM} = 27\,342$$

$$\text{LCM} = 1\,560$$

c) 50, 36 and 100

$$50 = 2 \times 5 \times 5$$

$$36 = 2 \times 2 \times 3 \times 3$$

$$100 = 2 \times 2 \times 5 \times 5$$

d) 22, 33 and 88

$$22 = 2 \times 11$$

$$33 = 3 \times 11$$

$$88 = 2 \times 2 \times 2 \times 11$$

$$\text{LCM} = 2 \times 2 \times 3 \times 3 \times 5 \times 5$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 \times 11$$

$$\text{LCM} = 900$$

$$\text{LCM} = 264$$

e) 16, 24 and 48

$$16 = 2 \times 2 \times 2 \times 2$$

$$24 = 2 \times 2 \times 2 \times 3$$

f) 91, 343 and 210

$$91 = 7 \times 13$$

$$343 = 7 \times 7 \times 7$$



$$48 = 2 \times 2 \times 2 \times 2 \times 3$$

$$\text{LCM} = 2 \times 2 \times 2 \times 2 \times 3$$

$$\text{LCM} = 48$$

$$210 = 2 \times 3 \times 5 \times 7$$

$$\text{LCM} = 2 \times 3 \times 5 \times 7 \times 7 \times 7 \times 13$$

$$\text{LCM} = 133\ 770$$

g) 228, 285 and 399

$$228 = 2 \times 2 \times 3 \times 19$$

$$285 = 3 \times 5 \times 19$$

$$399 = 3 \times 7 \times 19$$

$$\text{LCM} = 2 \times 2 \times 3 \times 5 \times 7 \times 19$$

$$\text{LCM} = 7\ 980$$

h) 60, 144 and 336

$$60 = 2 \times 2 \times 3 \times 5$$

$$144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3$$

$$336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7$$

$$\text{LCM} = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 7$$

$$\text{LCM} = 5\ 040$$

i) 255, 102 and 306

$$255 = 3 \times 5 \times 17$$

$$102 = 2 \times 3 \times 17$$

$$306 = 2 \times 3 \times 3 \times 17$$

$$\text{LCM} = 2 \times 3 \times 3 \times 5 \times 17$$

$$\text{LCM} = 1\ 530$$

j) 290, 580 and 145

$$290 = 2 \times 5 \times 29$$

$$580 = 2 \times 2 \times 5 \times 29$$

$$145 = 5 \times 29$$

$$\text{LCM} = 2 \times 2 \times 5 \times 29$$

$$\text{LCM} = 580$$